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LION-HUNTING WITH LOGIC*

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Over the years there has developed a body of literature on the use of mathematical techniques to catch lions ([1]–[6]). In this literature there has been a comparative shortage of proofs based on mathematical logic. If those of us who commit logic believe in the vitality of our field, we cannot afford to allow such a shortage to continue. The following proofs, then, are offered as a first step towards rectifying the situation.

1. *Nonstandard Analysis*. In a nonstandard universe (namely, the land of Oz [7]), lions are cowardly and may be caught easily. By the transfer principle, this likewise holds in our (standard) universe.

2. *Set Theory*. If the set of lions is bounded, you can simply build a cage around the boundary. So assume that the set of lions is unbounded. It will then have an element in common with a stationary set. But a stationary lion is trivial to capture.

3. *Set Theory*. Assume $V = L$. Since the lion is in the universe, it is constructible. So just carry out its construction within a cage in the first place.

4. *Set Theory*. Assume AC. Perform a Tarski-Banach decomposition on the lion to halve its size. Repeat until the lion is small enough to be captured easily.

5. *Recursion Theory*. Assume you can capture a lion. Having done so, you can easily bring it to a standstill, and you would thus have a solution to the halting problem. Since the halting problem is unsolvable, you *cannot* capture a lion after all.

In conjunction with the previous results, we have

COROLLARY. *Mathematics is inconsistent.*

This corollary, besides being of intrinsic interest, also provides solutions to the Riemann Hypothesis, Fermat's Last Theorem, and other questions (besides giving a proof of the Four-Color Theorem that does not require a computer!).

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*This research received compact support from Tombs grant LWH-42755.